DATA20021

University of Helsinki, Department of Computer Science

Information Retrieval

Lecture 6: Ranked Retrieval

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Today's lecture...

- 16.1: Introduction to Indexing
 - Boolean Retrieval model
 - Inverted Indexes
- 21.1: Index Compression
 - unary, gamma, variable-byte coding
 - (Partitioned) Elias-Fano coding (used by Google, facebook)
- 23.1: Index Construction
 - preprocessing documents prior to search
 - building the index efficiently
- 28.1: Web Crawling
 - getting documents off the web at scale
 - architecture of a large scale web search engine
- 30.1: Ranked Retrieval/Query Processing
 - Vector-Space model
 - scoring and ranking search results

Boolean retrieval

- Thus far, our queries have all been Boolean.
 - Documents either match or don't.
- Good for expert users with precise understanding of their needs and the collection.
 - Also good for programs: Programs can easily consume 1000s of results.
- Not good for the majority of users.
 - Most users incapable of writing Boolean queries (or they are, but they think it's too much work).
 - Most users don't want to wade through 1000s of results.
 - This is particularly true of web search.

Problem with Boolean search: feast or famine

- Boolean queries often result in either too few (=0) or too many (1000s) results.
- Query 1: "standard user dlink 650" \rightarrow 200,000 hits
- Query 2: "standard user dlink 650 no card found": 0 hits
- It takes a lot of skill to come up with a query that produces a manageable number of hits.
 - AND gives too few; OR gives too many

Ranked retrieval models

- Rather than a set of documents satisfying a query expression, in ranked retrieval, the system returns an ordering over the (top) documents in the collection for a query
- Free text queries: Rather than a query language of operators and expressions, the user's query is just one or more words in natural language
- Really, these are two separate things, but in practice, ranked retrieval has normally been associated with free text queries and vice versa

Feast or famine: not a problem in ranked retrieval

- When a system produces a ranked result set, large result sets are not an issue
 - Indeed, the size of the result set is not an issue
 - We just show the top k (\approx 10) results
 - We don't overwhelm the user
- Premise: the ranking algorithm works

Scoring as the basis of ranked retrieval

- We want to return *in order* the documents that are most likely to be useful to the searcher
- How can we rank-order the documents in the collection with respect to a query?
- Assign a score say in [0, 1] to each document
- This score measures how well document and query "match".

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Take 1: Jaccard coefficient

- A common measure of overlap of two sets A and B
- jaccard(A,B) = $|A \cap B| / |A \cup B|$
- jaccard(A,A) = 1
- jaccard(A,B) = 0 if $A \cap B$ = 0
- Always assigns a number between 0 and 1.
- A and B don't have to be the same size.

Jaccard coefficient: Scoring example

- What is the query-document match score that the Jaccard coefficient computes for each of the two documents below?
- Query: ides of march
- Document 1: caesar died in march
- Document 2: the long march

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Issues with Jaccard for scoring

- It doesn't consider *term frequency* (how many times a term occurs in a document)
- Rare terms in a collection are more informative than frequent terms. Jaccard doesn't consider this information
- We also need a more sophisticated way of normalizing for length

Query-document matching scores

- We need a way of assigning a score to a query/document pair
- Let's start with a one-term query
- If the query term does not occur in the document: score should be 0
- The more frequent the query term in the document, the higher the score (should be)
- We will look at a number of alternatives that capture these criteria...

Recall (Lecture 2): Binary termdocument incidence matrix

	Antony and Cleopatra	Julius Caesar	The Tempest	Hamlet	Othello	Macbeth
Antony	1	1	0	0	0	1
Brutus	1	1	0	1	0	0
Caesar	1	1	0	1	1	1
Calpurnia	0	1	0	0	0	0
Cleopatra	1	0	0	0	0	0
mercy	1	0	1	1	1	1
worser	1	0	1	1	1	0

Each document is represented by a binary vector $\in \{0,1\}^{|V|}$

Term-document count matrices

- Consider the number of occurrences of a term in a document:
 - Each document is a count vector in N^v: a column below

	Antony and Cleopatra	Julius Caesar	The Tempest	Hamlet	Othello	Macbeth
Antony	157	73	0	0	0	0
Brutus	4	157	0	1	0	0
Caesar	232	227	0	2	1	1
Calpurnia	0	10	0	0	0	0
Cleopatra	57	0	0	0	0	0
mercy	2	0	3	5	5	1
worser	2	0	1	1	1	0

Bag of words model

- Vector representation doesn't consider the ordering of words in a document
- This is called the <u>bag of words</u> model.
- John is quicker than Mary and Mary is quicker than John have the same vectors

Term frequency tf

- The term frequency tf_{t,d} of term t in document d is defined as the number of times that t occurs in d.
- We want to use tf when computing query-document match scores. But how?
- Raw term frequency is not what we want:
 - A document with 10 occurrences of the term is more relevant than a document with 1 occurrence of the term.
 - But not 10 times more relevant.
- Relevance does not increase proportionally with term frequency.

Log-term-frequency weighting

- The log frequency weight of term t in d is $w_{t,d} = \begin{cases} 1 + \log_{10} tf_{t,d}, & \text{if } tf_{t,d} > 0 \\ 0, & \text{otherwise} \end{cases}$
- $0 \rightarrow 0, 1 \rightarrow 1, 2 \rightarrow 1.3, 10 \rightarrow 2, 1000 \rightarrow 4$, etc.
- Score for a document-query pair: sum over terms t in both q and d:
- score $= \sum_{t \in q \cap d} (1 + \log tf_{t,d})$
- The score is 0 if none of the query terms is present in the document.

Rare terms are more informative

- Rare terms are more informative than frequent terms
 - Recall stop words
- Consider a term in the query that is rare in the collection (e.g., *arachnocentric*)
- A document containing this term is very likely to be relevant to the query *arachnocentric*
- → We want a high weight for rare terms like arachnocentric.

idf weight

- df_t is the <u>document</u> frequency of t: the number of documents that contain t
 - df_t is an inverse measure of the informativeness of t
 - $df_t \leq N$, the number of documents in the collection
- We define the idf (inverse document frequency) of t by $idf_t = log_{10} (N/df_t)$
 - We use log (N/df_t) instead of N/df_t to "dampen" the effect of idf.

idf example, suppose N = 1 million

term	df _t	idf _t
calpurnia	1	6
animal	100	4
sunday	1,000	3
fly	10,000	2
under	100,000	1
the	1,000,000	0

$$\mathrm{idf}_t = \log_{10} \left(N/\mathrm{df}_t \right)$$

We compute one idf value for each term t in a collection.

Collection vs. Document frequency

- Collection frequency of t is the number of occurrences of t in the collection
- Document frequency of t is the number of documents in which t occurs

Example:

Word	Collection frequency	Document frequency
insurance	10440	3997
try	10422	8760

Which word is better for search (gets higher weight)?

Effect of idf on ranking

- For the query <u>capricious person</u>, idf weighting makes occurrences of <u>capricious</u> count for much more in the final document ranking than occurrences of person.
- idf has no effect on ranking one term queries
 - idf affects the ranking of documents for queries with at least two terms

Sec. 6.2.2

tf-idf weighting

tf-idf weighting

 The tf-idf weight of a term is the product of its tf weight and its idf weight.

$$\mathbf{w}_{t,d} = \log(1 + \mathrm{tf}_{t,d}) \times \log_{10}(N/\mathrm{df}_t)$$

- Best known weighting scheme in information retrieval
 - Note: the "-" in tf-idf is a hyphen, not a minus sign
 - Alternative names: tf.idf, tf x idf
- Increases with the number of occurrences within a document
- Increases with the rarity of the term in the collection

Score for a document given a query

Score(q,d) =
$$\sum_{t \in q \cap d} \text{tf.idf}_{t,d}$$

There are many variants

- How "tf" is computed (with/without logs)
- Whether the terms in the query are also weighted

Binary \rightarrow count \rightarrow weight matrix

	Antony and Cleopatra	Julius Caesar	The Tempest	Hamlet	Othello	Macbeth
Antony	5.25	3.18	0	0	0	0.35
Brutus	1.21	6.1	0	1	0	0
Caesar	8.59	2.54	0	1.51	0.25	0
Calpurnia	0	1.54	0	0	0	0
Cleopatra	2.85	0	0	0	0	0
mercy	1.51	0	1.9	0.12	5.25	0.88
worser	1.37	0	0.11	4.15	0.25	1.95

Each document is now represented by a real-valued vector of tf-idf weights $\in \mathbb{R}^{|V|}$

Documents as vectors

- So we have a |V|-dimensional vector space
- Terms are axes of the space
- Documents are points or vectors in this space
- Very high-dimensional: tens of millions of dimensions when you apply this to a web search engine
- These are very sparse vectors most entries are zero.

Queries as vectors

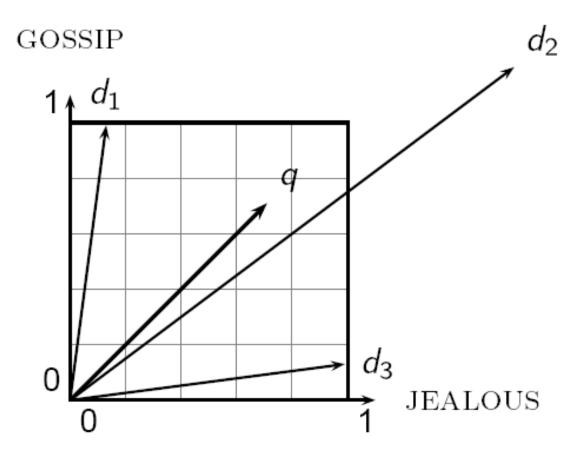
- Key idea 1: Do the same for queries: represent them as vectors in the space
- Key idea 2: Rank documents according to their proximity to the query in this space
- proximity = similarity of vectors
- proximity ≈ inverse of distance

Formalizing vector space proximity

- First thought: distance between two points
 - (= distance between the end points of the two vectors)
- Euclidean distance?
- Euclidean distance is a bad idea . . .
- ... because Euclidean distance is large for vectors of different lengths.

Why distance is a bad idea

The Euclidean distance between q and $\vec{d_2}$ is large even though the distribution of terms in the query \vec{q} and the distribution of terms in the document $\vec{d_2}$ are very similar.



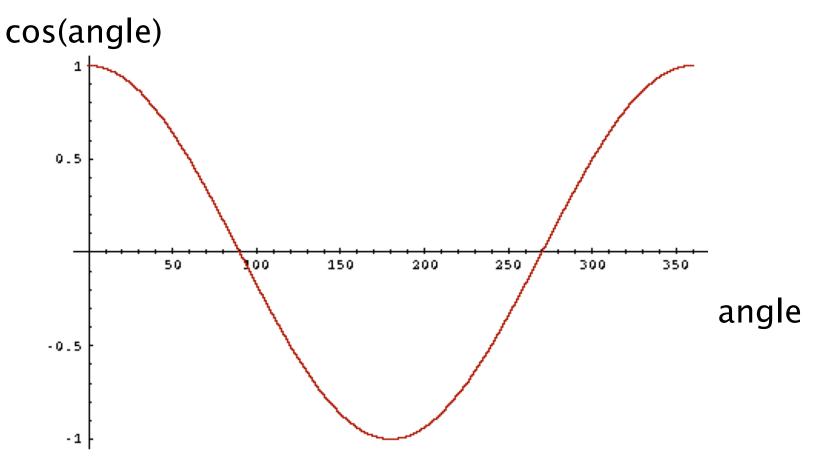
Use angle instead of distance

- Thought experiment: take a document d and append it to itself. Call this document d'.
- "Semantically" d and d' have the same content
- The Euclidean distance between the two documents can be quite large
- The angle between the two documents is 0, corresponding to maximal similarity.
- Key idea: Rank documents according to angle with query.

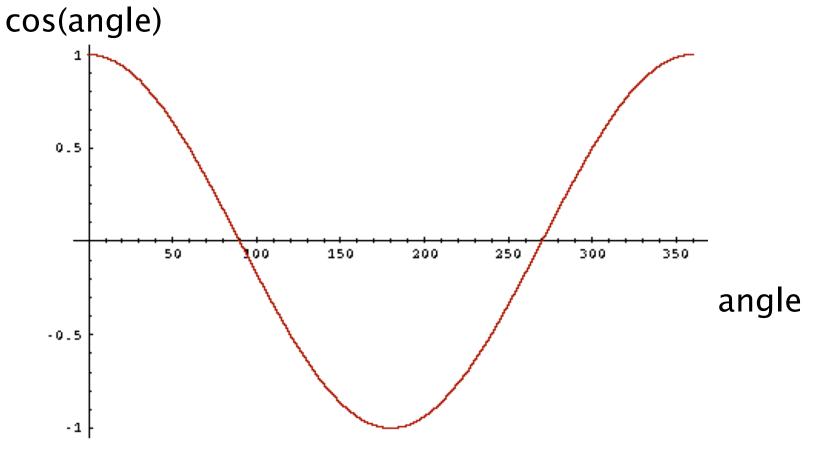
Deriving a score: from angles to cosines

- The following two notions are equivalent.
 - Rank documents in <u>decreasing</u> order of the angle between query and document (lower angle = better match)
 - Rank documents in <u>increasing</u> order of cosine(query,document) (lower angle = higher cos(angle))
- Cosine is a monotonically decreasing function for the interval [0°, 180°]
 - <u>Using cos(angle) as score for document means documents</u> <u>having lower angle with query get higher scores</u>

From angles to cosines (angle \uparrow cos \downarrow)



From angles to cosines (angle \uparrow cos \downarrow)



How do we compute the cosine of two vectors?

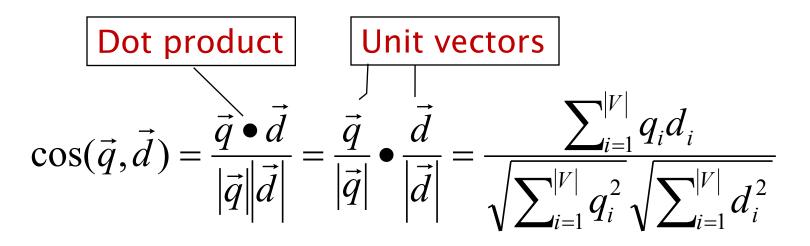
First: Length normalization

• A vector can be (length-) normalized by dividing each of its components by its length – for this we use the L_2 norm: $\|\vec{x}\| = \sqrt{\sum x^2}$

$$\left\|\vec{x}\right\|_2 = \sqrt{\sum_i x_i^2}$$

- Dividing a vector by its L₂ norm makes it a unit (length) vector (on surface of unit hypersphere)
- Long and short documents now have comparable weights
- Effect on the two documents d and d' (d appended to itself) from earlier slide: they have identical vectors after length-normalization.

cosine(query,document)



 q_i is the weight of term *i* in the query d_i is the weight of term *i* in the document

 $\cos(\vec{q}, \vec{d})$ is the cosine similarity of \vec{q} and \vec{d} ... or, equivalently, the cosine of the angle between \vec{q} and \vec{d} .

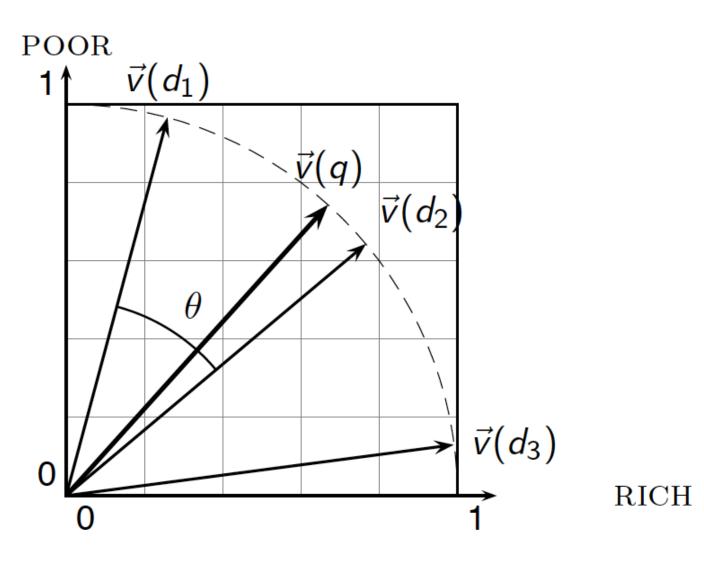
Cosine for length-normalized vectors

For length-normalized vectors, cosine similarity is simply the dot product (or scalar product):

$$\cos(q,d) = q \bullet d = \sum_{i=1}^{|V|} q_i d_i$$

for q, d length-normalized.

Cosine similarity illustrated



Cosine similarity amongst 3 documents

How similar are

the novels SaS: Sense and Sensibility PaP: Pride and *Prejudice*, and WH: Wuthering Heights?

term	SaS	PaP	WH	
affection	115	58	20	
jealous	10	7	11	
gossip	2	0	6	
wuthering	0	0	38	

Term frequencies (counts)

Note: To simplify this example, we don't do idf weighting.

	term	SaS	PaP	WH
Term frequencies (counts)	affection	115	58	20
	jealous	10	7	11
	gossip	2	0	6
	wuthering	0	0	38

Log frequency weighting

After length normalization

term	SaS	PaP	WH
affection	3.06	2.76	2.30
jealous	2.00	1.85	2.04
gossip	1.30	0	1.78
wuthering	0	0	2.58

dot(SaS,PaP) \approx 12.1 dot(SaS,WH) \approx 13.4 dot(PaP,WH) \approx 10.1

term	SaS	PaP	WH
affection	0.789	0.832	0.524
jealous	0.515	0.555	0.465
gossip	0.335	0	0.405
wuthering	0	0	0.588

 $cos(SaS,PaP) \approx 0.94$ $cos(SaS,WH) \approx 0.79$ $cos(PaP,WH) \approx 0.69$

Computing cosine scores

$\operatorname{COSINESCORE}(q)$

- 1 float Scores[N] = 0
- 2 float Length[N]
- 3 for each query term t
- 4 **do** calculate $w_{t,q}$ and fetch postings list for t
- 5 **for each** $pair(d, tf_{t,d})$ in postings list
- 6 **do** $Scores[d] + = w_{t,d} \times w_{t,q}$
- 7 Read the array Length
- 8 for each d
- 9 **do** Scores[d] = Scores[d]/Length[d]
- 10 return Top K components of Scores[]

Computing cosine scores

- Previous algorithm scores term-at-a-time (TAAT)
- Algorithm can be adapted to scoring document-at-atime (DAAT)
- Storing $w_{t,d}$ in each posting could be expensive
 - ...because we'd have to store a floating point number
 - For tf-idf scoring, it suffices to store tf_{t,d} in the posting and idf_t in the head of the postings list
- Extracting the top K items can be done with a heap
 - Lots of ways to optimize this for speed

tf-idf weighting has many variants

Term frequency		Docum	ent frequency	Normalization		
n (natural)	$tf_{t,d}$	n (no)	1	n (none)	1	
l (logarithm)	$1 + \log(tf_{t,d})$	t (idf)	$\log \frac{N}{df_t}$	c (cosine)	$\frac{1}{\sqrt{w_1^2 + w_2^2 + + w_M^2}}$	
a (augmented)	$0.5 + \frac{0.5 \times \text{tf}_{t,d}}{\max_t(\text{tf}_{t,d})}$	p (prob idf)	$\max\{0, \log \frac{N - \mathrm{df}_t}{\mathrm{df}_t}\}$	u (pivoted unique)	1/ <i>u</i>	
b (boolean)	$egin{cases} 1 & ext{if } \operatorname{tf}_{t,d} > 0 \ 0 & ext{otherwise} \end{cases}$			b (byte size)	$1/\mathit{CharLength}^lpha$, $lpha < 1$	
L (log ave)	$\frac{1 + \log(\operatorname{tf}_{t,d})}{1 + \log(\operatorname{ave}_{t \in d}(\operatorname{tf}_{t,d}))}$					

Weighting may differ in queries vs documents

- Many search engines allow for different weightings for queries vs. documents
- SMART Notation: denotes the combination in use in an engine, with the notation *ddd.qqq*, using the acronyms from the previous table
- A very standard weighting scheme is: Inc.ltc
- Document: logarithmic tf (I as first character), no idf and cosine normalization
- Query: logarithmic tf (I in leftmost column), idf (t in second column), cosine normalization ...

tf-idf example: Inc.Itc

Document: *car insurance auto insurance* Query: *best car insurance*

Term	Query				Document			product		
	tf- raw	tf-wt	df	idf	wt	tf-raw	tf-wt	wt	n'lized	
auto	0	0	5000	2.3	0	1	1	1	0.52	0
best	1	1	50000	1.3	1.3	0	0	0	0	0
car	1	1	10000	2.0	2.0	1	1	1	0.52	0.27
insurance	1	1	1000	3.0	3.0	2	1.3	1.3	0.68	0.53

Summary – vector space ranking

- Represent the query as a weighted tf-idf vector
- Represent each document as a weighted tf-idf vector
- Compute the cosine similarity score for the query vector and each document vector
- Rank documents with respect to the query by score
- Return the top K (e.g., K = 10) to the user

Takeaway Today

- Ranking search results: why it is important (as opposed to just presenting a set of unordered Boolean results)
- Term frequency: This is a key ingredient for ranking.
- Tf-idf ranking: best known traditional ranking scheme
- Vector space model: Important formal model for information retrieval (along with Boolean and probabilistic models)

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Resources for today's lecture

- Exploring the Similarity Space, by Justin Zobel and Alistair Moffat – an excellent look at various TF.IDFbased measures
 - Google for article title, you'll find a free copy
- Chapter 6 of Manning et al. (Intro to IR):
 - <u>https://nlp.stanford.edu/IR-book/pdf/06vect.pdf</u>
- Also some practice in Exercise Set 3



<u>Tuesday, 4.2</u>: Evaluating IR Systems

- ...